

3.1 Fractions to Decimals

Non-integer numbers can be written as fraction or decimals.

Fractions:  $\frac{2}{5}$  ← numerator  
 ← denominator



Decimals: 0.625 ← thousandth  
 ↑ ↑  
 tenth hundredth

Fraction	$\frac{7}{10}$ seven tenths	$\frac{1}{100}$	$\frac{19}{100}$	$\frac{1}{1000}$	$\frac{23}{1000}$
Decimal	0.7	0.01	0.19	0.001	0.023

seven in the tenth spot

Example: Write each fraction as a decimal.

Strategy #1 – Change the fraction so that the denominator is 10, 100, 1000 etc.

$$\frac{3}{5} \xrightarrow{\times 2} \frac{6}{10} = 0.6$$

$$\frac{6}{25} \xrightarrow{\times 4} \frac{24}{100} = 0.24$$

end in the thousandth place

must do same to top & bottom

Strategy #2 – Divide using long division.

$$\begin{array}{r} 0.375 \\ 8 \overline{) 3.0000} \\ \underline{-24} \phantom{00} \\ 60 \phantom{0} \\ \underline{-56} \phantom{0} \\ 40 \\ \underline{-40} \\ 0 \end{array}$$

when you can't easily change the fraction

$$\frac{3}{8} = 0.375$$

Example: Write each decimal as a fraction. Reduce to lowest terms.

← simplify

$$\frac{0.73}{100} = \frac{73}{100}$$

can't reduce - no common factors

$$\frac{0.12}{100} \div 4 = \frac{12}{100} \div 4 = \frac{3}{25}$$

HW p. 88 # 1, 2, 3a, 4,  
 Bonus 5, 6, 8, 9, 10

## extension

Decimals such as 0.1 and 0.25, are terminating decimals.

Decimals such as 0.333 333... or 0.454 545...; 0.811 111... are repeating decimals.

Some digits in each repeating decimal repeat forever. We draw a bar over the digits that repeat.

Example:

$$0.\overline{3}$$

$$0.\overline{45}$$

$$0.\overline{81}$$

Use a calculator to divide the following:

$$5 \div 9$$

$$= 0.5$$

$$38 \div 99$$

$$0.\overline{38}$$

$$13 \div 999$$

$$0.\overline{013}$$

What pattern do you see?

# of repeating digits = the # of 9's  
in the denominator

Example: Write the following repeating decimals as fractions.

$$0.\overline{2} = \frac{2}{9}$$

$$0.\overline{875} = \frac{875}{999}$$

$$0.\overline{03} = \frac{3}{99}$$

# Mixed fraction

# Improper fraction

Math 7

NAME:

## 3.2 Comparing and Ordering Fractions and Decimals

Date:

Question: Three students are selling chocolate bars as a fund raiser for their school. The bars are packaged in cartons. Ardavan sold  $2\frac{2}{3}$  cartons, Isha sold  $\frac{5}{2}$  cartons and Daniel sold 2.25 cartons.

Who sold the most chocolate bars? How do you know?

Ardavan



$$2\frac{2}{3}$$

Isha



$$\frac{5}{2} = 2\frac{1}{2}$$

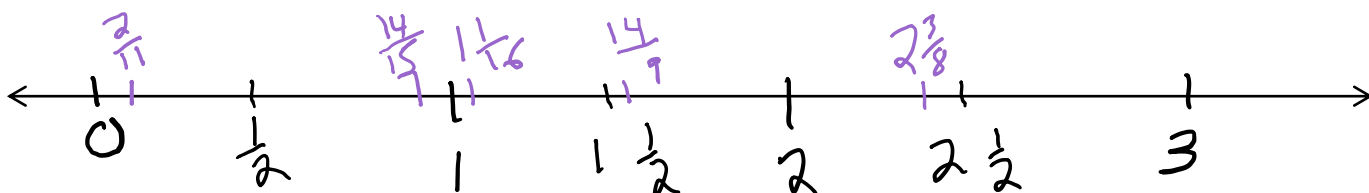
Daniel



$$2.25 = 2\frac{25}{100} = 2\frac{1}{4}$$

Any fraction greater than 1 can be written as a mixed number.

Use a number line to order the following numbers:  $\frac{2}{11}$ ,  $2\frac{3}{8}$ ,  $1\frac{1}{16}$ ,  $\frac{14}{9}$ ,  $\frac{14}{15}$



Example:

a) Write the following numbers in order from least to greatest:  $\frac{7}{8}$ ,  $\frac{9}{8}$ ,  $\frac{1}{4}$ , 0.75

$$\frac{1}{4} \times 2 = \frac{2}{8}$$

$$0.75 = \frac{75}{100} \div 25 = \frac{3}{4} \times 2 = \frac{6}{8}$$

same denominator

$$\frac{2}{8}, \frac{6}{8}, \frac{7}{8}, \frac{9}{8}$$

$$\frac{1}{4}, 0.75, \frac{7}{8}, \frac{9}{8}$$

b) Write a number between  $\frac{9}{8}$  and  $1\frac{1}{4}$ .

$$1\frac{1}{4} = \frac{5}{4}$$

$$\frac{9}{8}$$

$$\frac{5}{4} \times 2 = \frac{10}{8}$$

$$\frac{9}{8} \times 2 = \frac{18}{8}$$

$$\frac{10}{8} \times 2 = \frac{20}{8}$$

$$\frac{18}{16}, \frac{19}{16}, \frac{20}{16}$$

HW: p. 94

# 1, 3ac, 4ac, 5a, 6, 7, 8ac, 9a, 10, 11 2 days

3.3 Adding and Subtracting Decimals

The Hunger Games: Mockingjay just set box office records for an opening 5 days in November. The earnings are shown in the table.

**Estimate** the total box office earnings.

$$\begin{aligned}
 70.95 &\rightarrow 71 \\
 52.6 &\rightarrow 53 \\
 34.53 &\rightarrow 35 \\
 12.3 &\rightarrow 12 \\
 15.9 &\rightarrow 16
 \end{aligned}$$

$$\begin{array}{r}
 71 \\
 53 \\
 35 \\
 12 \\
 16 \\
 \hline
 187
 \end{array}$$

Day	Earnings (Millions of \$)
Friday	70.95
Saturday	52.6
Sunday	34.53
Monday	12.3
Tuesday	15.9

Tips on Rounding:

- Find the place that you want to round
- Look at the digit to the right
- If it is 0 – 4 round down
- If it is 5 – 9 round up

When adding or subtracting decimal we will always estimate the answer first.

Determine the exact box office earnings.

$$\begin{array}{r}
 70.95 \\
 52.60 \\
 34.53 \\
 12.30 \\
 15.90 \\
 \hline
 186.28
 \end{array}$$

$$\$186.28$$

How **much more money** did the movie make on Friday than it did on Saturday?

$$\begin{array}{r}
 70.95 \\
 - 52.60 \\
 \hline
 18.35
 \end{array}$$

$$\$18.35$$

Homework: p.98 # 1-6, 9,10

Estimate the following:

1)  $13.7 + 9.15$

$$\begin{aligned}
 14 + 9 \\
 = 23
 \end{aligned}$$

2)  $14.63 + 122.1$

$$\begin{array}{r}
 15 + 122 \\
 122 \\
 + 15 \\
 \hline
 137
 \end{array}$$

3)  $48.3 - 12.59$

$$\begin{aligned}
 48 - 13 \\
 = 35
 \end{aligned}$$

4)  $263.94 - 32.87$

$$\begin{array}{r}
 264 - 33 \\
 264 \\
 - 33 \\
 \hline
 231
 \end{array}$$

3.4 Multiplying Decimals

Calculate the following:

12 x 22

$$\begin{array}{r}
 12 \\
 \times 22 \\
 \hline
 24 \\
 +240 \\
 \hline
 264
 \end{array}$$

38 x 11

$$\begin{array}{r}
 38 \\
 \times 11 \\
 \hline
 38 \\
 +380 \\
 \hline
 418
 \end{array}$$

Estimate the following:

1.9 x 2.3

2 x 2 = 4

4.25 x 9.11

4 x 9 = 36

12.2195 x 8.5903

only care about # next to column we want to round to

12 x 9 = 108 to column

We can solve decimal multiplication by estimating and then calculating

Ex: 8.7 x 3.4

9 x 3 = 27

$$\begin{array}{r}
 8.7 \\
 \times 3.4 \\
 \hline
 348 \\
 +2610 \\
 \hline
 2958
 \end{array}$$

29.58

use estimate to help place decimal

2) 2.28 x 15.6

2 x 16 = 32

$$\begin{array}{r}
 2.28 \\
 \times 15.6 \\
 \hline
 1368 \\
 11400 \\
 22800 \\
 \hline
 35528
 \end{array}$$

don't need decimal places to line up

35568

where to put decimal that is close to 32?

Homework: p. 102 # 8- 13

To determine where to place the decimal point in our answer we can do the following:

- Look at our original numbers

Count the number of digits after the decimal place in the original number and then make sure that there are the same total number of digits

3.5 Dividing by Decimals

Ex.  $52.1 \div 0.8$

Use a calculator to find the following:

1)  $52.1 \div 10$

2)  $52.1 \div 50$

3)  $52.1 \div 100$

When we divide by a number greater than one the dividend gets \_\_\_\_\_.

Use a calculator to find the following:

1)  $52.1 \div 0.1$

2)  $52.1 \div 0.05$

3)  $52.1 \div 0.01$

When we divide by a number less than one the dividend gets \_\_\_\_\_.

Homework: p. 106 # 2-10 Bonus 11-13

3.6 Order of Operations

- When solving equations with multiple operations we go \_\_\_\_\_
- Remember that we need to solve it in the correct order: \_\_\_\_\_

Ex: Solve  $12.376 \div (4.75 + 1.2) + 2.45 \times 0.2 - 1.84$

B  
E  
D  
M  
A  
S

## 3.7 Relating Fractions, Decimals and Percents

Percentages are another way to write \_\_\_\_\_ and \_\_\_\_\_.

Ex: 12%

85%

**En Francais:**

Hundred = \_\_\_\_\_

So **percent** literally translates to:

Write the following as fractions and decimals:

a) 75%

b) 8%

c) 157%

Strategy for converting percentages:

- Write the number over \_\_\_\_\_ •

Write the following as percentages:

a) 0.18

b) 0.7

c)  $\frac{7}{25}$

d)  $\frac{21}{35}$

Strategy for converting to percentage

- Write as a fraction with a denominator of \_\_\_\_\_.
- If you are stuck \_\_\_\_\_ the fraction first.

**Homework: p.112 # 1-5**



**3.8 Solving Percentage Problems**

Ex: A jacket costs \$48 and is on sale for 30% off.

- a. How much would you save?
- b. What is the final cost of the jacket?

**Estimate**

Ex: A book costs \$9 and there is an 8% sales tax. What is the final sale price?

**Estimate**